

Abstract

Let $Q_n(x; \beta, \gamma, c)$ be the polynomials of degree n which satisfy the recurrence relation:

$$\begin{aligned} a_{n+c}Q_{n+1}(x; \beta, \gamma, c) + a_{n+c-1}Q_{n-1}(x; \beta, \gamma, c) + (\beta_{n+c} + \beta\delta_{n,0})Q_n(x; \beta, \gamma, c) \\ = x(1 + (\gamma - 1)\delta_{n,0})Q_n(x; \beta, \gamma, c), \\ Q_{-1}(x; \beta, \gamma, c) = 0, \quad Q_0(x; \beta, \gamma, c) = 1. \end{aligned}$$

In the above, β is real, $\gamma > 0$, a_{n+c} and β_{n+c} are real sequences with $a_{n+c} > 0$, and $\delta_{n,0}$ is the Kronecker symbol. The co-recursive associated orthogonal polynomials are obtained from the above for $\gamma = 1$.

In this paper, the Newton sum rules for the k th power of the zeros of scaled co-recursive associated orthogonal polynomials are determined in terms of the Newton sum rules of associated orthogonal polynomials. Some monotonicity properties of the zeros also are given.