

# BOOK OF ABSTRACTS

The 3<sup>rd</sup> International Conference  
and Summer School  
**Numerical Computations:  
Theory and Algorithms**  
**NUMTA 2019**



edited by

Yaroslav D. Sergeyev  
Dmitri E. Kvasov  
Marat S. Mukhametzhanov  
Maria Chiara Nasso

UNIVERSITÀ DELLA CALABRIA

**Centro Editoriale e Librario**



University of Calabria, Rende (CS), Italy  
in cooperation with  
Society for Industrial and Applied Mathematics, USA

**Book of Abstracts  
of the 3rd International Conference  
and Summer School**

**Numerical Computations:  
Theory and Algorithms**

edited by  
**Yaroslav D. Sergeyev  
Dmitri E. Kvasov  
Marat S. Mukhametzhanov  
Maria Chiara Nasso**

**Le Castella - Isola Capo Rizzuto  
Crotone, Italy  
June 15-21, 2019**

**UNIVERSITÀ DELLA CALABRIA  
Centro Editoriale e Librario**



## Scientific Committee

Lidia Aceto, Italy  
Andy Adamatzky, UK  
Francesco Archetti, Italy  
Thomas Bäck, Netherlands  
Roberto Battiti, Italy  
Roman Belavkin, UK  
Giancarlo Bigi, Italy  
Paola Bonizzoni, Italy  
Luigi Brugnano, Italy  
Sergiy Butenko, USA  
Sonia Cafieri, France  
Tianxin Cai, China  
Cristian Calude, New Zealand  
Antonio Candelieri, Italy  
Mario Cannataro, Italy  
Giovanni Capobianco, Italy  
Domingos Cardoso, Portugal  
Francesco Carrabs, Italy  
Emilio Carrizosa, Spain  
Leocadio Casado, Spain  
Carmine Cerrone, Italy  
Raffaele Cerulli, Italy  
Marco Cococcioni, Italy  
Salvatore Cuomo, Italy  
Louis D'Alotto, USA  
Oleg Davydov, Germany  
Renato De Leone, Italy  
Alessandra De Rossi, Italy  
Kalyanmoy Deb, USA  
Francesco Dell'Accio, Italy  
Branko Dragovich, Serbia  
Gintautas Dzemyda, Lithuania  
Yalchin Efendiev, USA  
Michael Emmerich, Netherlands  
Adil Erzin, Russia  
Yury Evtushenko, Russia  
Giovanni Fasano, Italy  
Şerife Faydaoğlu, Turkey  
Luca Formaggia, Italy  
Elisa Francomano, Italy  
Masao Fukushima, Japan  
David Gao, Australia  
Manlio Gaudioso, Italy  
Victor Gergel, Russia  
Jonathan Gillard, UK  
Daniele Gregori, Italy  
Vladimir Grishagin, Russia  
Mario Guarracino, Italy  
Nicola Guglielmi, Italy  
Jan Hesthaven, Switzerland  
Felice Iavernaro, Italy  
Mikhail Khachay, Russia  
Oleg Khamisov, Russia  
Timos Kipouros, UK  
Lefteris Kirousis, Greece  
Yury Kochetov, Russia  
Olga Kostyukova, Belarus  
Vladik Kreinovich, USA  
Dmitri Kvasov, Italy  
Hoai An Le Thi, France  
Wah June Leong, Malaysia  
Øystein Linnebo, Norway  
Antonio Liotta, UK  
Marco Locatelli, Italy  
Stefano Lucidi, Italy  
Maurice Margenstern, France  
Vladimir Mazalov, Russia  
Francesca Mazzia, Italy  
Maria Mellone, Italy  
Kaisa Miettinen, Finland  
Edmondo Minisci, UK  
Nenad Mladenovic, Serbia  
Ganesan Narayanasamy, USA  
Ivo Nowak, Germany  
Donatella Occorsio, Italy  
Marco Panza, USA  
Massimo Pappalardo, Italy  
Panos Pardalos, USA  
Remigijus Paulavičius, Lithuania  
Hoang Xuan Phu, Vietnam  
Stefan Pickl, Germany  
Raffaele Pisano, France  
Yuri Popkov, Russia  
Mikhail Posypkin, Russia  
Oleg Prokopyev, USA  
Davide Rizza, UK  
Massimo Roma, Italy  
Valeria Ruggiero, Italy  
Maria Grazia Russo, Italy  
Nick Sahinidis, USA  
Leonidas Sakalauskas, Lithuania  
Yaroslav Sergeyev, Italy (Chair)  
Khodr Shamseddine, Canada  
Sameer Shende, USA  
Vladimir Shylo, Ukraine  
Theodore Simos, Greece  
Vinai Singh, India  
Majid Soleimani-Damaneh, Iran  
William Spataro, Italy  
Maria Grazia Speranza, Italy  
Giandomenico Spezzano, Italy  
Rosamaria Spitaleri, Italy  
Alexander Strekalovskiy, Russia  
Roman Strongin, Russia  
Gopal Tadepalli, India  
Tatiana Tchemisova, Portugal  
Gerardo Toraldo, Italy  
Vassili Toropov, UK  
Hiroshi Umeo, Japan  
Michael Vrahatis, Greece  
Song Wang, Australia  
Gerhard-Wilhelm Weber, Poland  
Luca Zanni, Italy  
Anatoly Zhigljavsky, UK  
Antanas Žilinskas, Lithuania  
Julius Žilinskas, Lithuania  
Joseph Zyss, France

## Organizing Committee

Francesco Dall'Accio (Rende, Italy)  
(SIAM representative)  
Alfredo Garro (Rende, Italy)  
Vladimir Grishagin (Nizhni Novgorod, Russia)  
Dmitri Kvasov (Rende, Italy)  
Marat Mukhametzhanov (Rende, Italy)  
Maria Chiara Nasso (Rende, Italy)  
Clara Pizzuti (Rende, Italy)  
Davide Rizza (Norwich, UK)  
Yaroslav Sergeyev (Rende, Italy)

# Table of Contents

<b><i>Welcoming message of Chairman of NUMTA-2019</i></b> .....	<b>21</b>
<i>Yaroslav D. Sergeev</i>	
<b><i>Plenary lectures</i></b> .....	<b>23</b>
Infinite Games on Finite Graphs using Grossone.....	25
<i>Louis D’Alotto</i>	
Recent advances on the use of $\mathbb{1}$ in optimization and regularization problems ..	26
<i>Renato De Leone</i>	
Karush-Kuhn-Tucker Proximity Measure for Convergence of Real-parameter Single and Multi-Objective Optimization .....	27
<i>Kalyanmoy Deb</i>	
Numerical modeling of flow in fractured porous media and fault reactivation ...	28
<i>Luca Formaggia, Anna Scotti</i>	
Precision Algorithms .....	29
<i>Jan S. Hesthaven and Deep Ray</i>	
Numerical differentiation on the Infinity Computer and applications for solving ODEs and approximating functions .....	30
<i>Francesca Mazzia</i>	
Generalizations of the intermediate value theorem for approximations of fixed points and zeroes of continuous functions .....	31
<i>Michael N. Vrahatis</i>	
Uniformly distributed sequences and space-filling .....	32
<i>Anatoly Zhigljavsky</i>	
<b><i>Tutorials</i></b> .....	<b>33</b>
Vector kinetic approximations to fluid-dynamics equations .....	35
<i>Roberta Bianchini, Roberto Natalini</i>	
Grossone-based Infinity Computing with Numerical Infinities and Infinitesimals.	36
<i>Yaroslav D. Sergeev</i>	
Design optimization techniques for industrial applications: challenges and progress .....	37
<i>Vassili Toropov</i>	
<b><i>Special sessions</i></b> .....	<b>39</b>
<b><i>Approximation: methods, algorithms and applications</i></b> .....	<b>41</b>
Laplace Transform Inversion for multiexponential decay data by smoothing L-splines .....	43
<i>Rosanna Campagna, Costanza Conti, Salvatore Cuomo</i>	
An Adaptive Refinement Scheme for Radial Basis Function Collocation.....	44
<i>Roberto Cavoretto, Alessandra De Rossi</i>	

# Plenary lectures

# Generalizations of the intermediate value theorem for approximations of fixed points and zeroes of continuous functions

Michael N. Vrahatis

Department of Mathematics, University of Patras, GR-26110 Patras, Greece  
vrahatis@math.upatras.gr

**Keywords.** Bolzano theorem; Bolzano-Poincaré-Miranda theorem; intermediate value theorems; existence theorems; fixed points; nonlinear equations; numerical optimization.

Generalizations of the tractional intermediate value theorem are presented. The obtained generalized theorems are particular useful for the existence of solutions of systems of nonlinear equations in several variables as well as for the existence of fixed points of functions and the localization and computation of extrema of objective functions.

The only computable information required by the numerical methods based on these generalized theorems is the algebraic sign of the function that is the smallest amount of information (one bit of information) necessary for the purpose needed, and not any additional information. Thus, these numerical methods are of major importance for tackling problems with imprecise (not exactly known) information. This kind of problems occurs in various scientific fields including mathematics, economics, engineering, computer science, biomedical informatics, medicine and bioengineering among others. This is so, because, in a large variety of applications, precise function values are either impossible or time consuming and computationally expensive to obtain.

Furthermore, these methods are particularly useful for tackling various problems where the corresponding functions take *very large* and/or *very small* values.

## References

- [1] Vrahatis M.N. (1988) Solving systems of nonlinear equations using the nonzero value of the topological degree. *ACM Transactions on Mathematical Software*, Vol. 14, pp. 312–329.
- [2] Vrahatis M.N. (1989) A short proof and a generalization of Miranda’s existence theorem. *Proceedings of the American Mathematical Society*, Vol. 107, pp. 701–703.
- [3] Vrahatis M.N. (1995) An efficient method for locating and computing periodic orbits of nonlinear mappings. *Journal of Computational Physics*, Vol. 119, pp. 105–119.
- [4] Vrahatis M.N. (2016) Generalization of the Bolzano theorem for simplices. *Topology and its Applications*, Vol. 202, pp. 40–46.